PROBLEM

1. Write the equation and graph a circle with center $(6,-3)$ containing the point $(3,-6)$.


ANS:
Circle: $(x-6)^{2}+(y+3)^{2}=18 \quad$ Center: $(6,-3) \quad r=4.24$


PTS: 1
2. Write the equation and graph a circle with center $(-6,4)$ containing the point $(-2,3)$.


ANS:
Circle: $(x+6)^{2}+(y-4)^{2}=17 \quad$ Center: $(-6,4) \quad r=4.12$


PTS: 1
3. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
x^{2}+y^{2}+10 x-12 y+52=0
$$



ANS:
Circle: $(x+5)^{2}+(y-6)^{2}=9 \quad$ Center: $(-5,6) \quad r=9$


PTS: 1
4. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
9 x^{2}+9 y^{2}-18 x+36 y-36=0
$$



ANS:
Circle: $(x-1)^{2}+(y+2)^{2}=9 \quad$ Center: $(1,-2) \quad r=3$


PTS: 1
5. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
9 x^{2}+36 y^{2}+108 x-432 y+1296=0
$$



ANS:
Ellipse: $\frac{(x+6)^{2}}{6^{2}}+\frac{(y-6)^{2}}{3^{2}}=1 \quad$ Center: $(-6,6) \quad a=6 \quad \mathrm{~b}=3$


PTS: 1
NOT: Major axis may be parallel to either the x - or y - axes.
6. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
25 x^{2}+9 y^{2}-300 x+90 y+900=0
$$



ANS:
Ellipse: $\frac{(x-6)^{2}}{3^{2}}+\frac{(y+5)^{2}}{5^{2}}=1 \quad$ Center: $(6,-5) \quad a=5 \quad \mathrm{~b}=3$


PTS: 1 NOT: Major axis is always parallel to the $y$-axis.
7. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
16 x^{2}+81 y^{2}+192 x-324 y-396=0
$$



ANS:
Ellipse: $\frac{(x+6)^{2}}{9^{2}}+\frac{(y-2)^{2}}{4^{2}}=1 \quad$ Center: $(-6,2) \quad a=9 \quad \mathrm{~b}=4$


PTS: 1 NOT: Major axis is always parallel to the x -axis.
8. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
36 x^{2}-100 y^{2}+216 x+800 y-4876=0
$$

ANS:
Hyperbola opening left-right: $\frac{(x+3)^{2}}{10^{2}}-\frac{(y-4)^{2}}{6^{2}}=1 \quad$ Center: $(-3,4) \quad a=10 \quad \mathrm{~b}=6$


PTS: 1
9. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
16 x^{2}-49 y^{2}-128 x-196 y+844=0
$$



ANS:
Hyperbola opening up-down: $\frac{(y+2)^{2}}{4^{2}}-\frac{(x-4)^{2}}{7^{2}}=1 \quad$ Center: (4,-2) $\quad a=7 \quad \mathrm{~b}=4$


PTS: 1
10. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
x=-5 y^{2}-40 y-77
$$



ANS:
Parabola opening left: Vertex: $(3,-4) \quad y$-intercept 1: $(0,-4.77)$ y-intercept 2: $(0,-3.23)$


PTS: 1
NOT: 2 y-intercepts: rational or irrational
11. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
x=-6 y^{2}-36 y-48
$$



ANS:
Parabola opening left: $\quad$ Vertex: $(6,-3) \quad y$-intercept 1: $(0,-4) \quad y$-intercept $2:(0,-2)$


PTS: 1
NOT: 2 y-intercepts: both rational
12. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
x=-y^{2}-2 y+4
$$



ANS:
Parabola opening left: $\quad$ Vertex: $(5,-1) \quad y$-intercept 1: $(0,-3.24)$ y-intercept 2: $(0,1.24)$


PTS: 1
NOT: 2 y -intercepts: both irrational
13. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
x=y^{2}-2 y 0
$$



ANS:
Parabola opening right: $\quad$ Vertex: $(-1,1)$


PTS: 1
14. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
x=6 y^{2}-12 y+3
$$

ANS:
Parabola opening right: $\quad$ Vertex: $(-3,1) \quad y$-intercept $1:(0,1.71) \quad y$-intercept $2:(0,0.29)$


PTS: 1
NOT: 2 y-intercepts: rational or irrational
15. Identify the shape of the graph, transform it into standard form, and sketch the graph indicating the most important parts.

$$
x=y^{2}-8 y+12
$$

ANS:
Parabola opening right: $\quad$ Vertex: $(-4,4)$ y-intercept $1:(0,6)$ y-intercept $2:(0,2)$


PTS: 1
NOT: 2 y-intercepts: both rational

